



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
 General Certificate of Education Ordinary Level

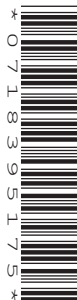
CANDIDATE
NAME

CENTRE
NUMBER

--	--	--	--	--

CANDIDATE
NUMBER

--	--	--	--



MATHEMATICS (SYLLABUS D)

4024/22

Paper 2

October/November 2011

2 hours 30 minutes

Candidates answer on the Question Paper.

Additional Materials: Geometrical instruments
 Electronic calculator

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO **NOT** WRITE IN ANY BARCODES.

Section A

Answer **all** questions.

Section B

Answer any **four** questions.

If working is needed for any question it must be shown in the space below that question.

Omission of essential working will result in loss of marks.

You are expected to use an electronic calculator to evaluate explicit numerical expressions.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 100.

For Examiner's Use

--

This document consists of **24** printed pages.



Section A [52 marks]Answer **all** questions in this section.*Do not
write in this
margin*

1 (a) $A = h(4m + h)$

Express m in terms of A and h .*Answer* [3]

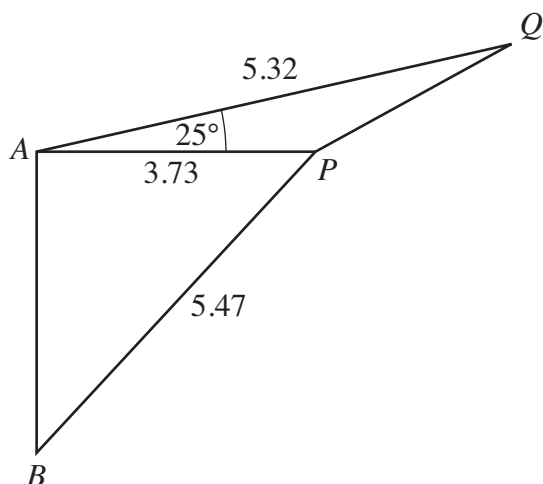
(b) Factorise completely $3ax + 5bx - 6ay - 10by$.

Answer [2]

(c) Solve the equation $\frac{5x-1}{9} = \frac{9}{5x-1}$.

Do not
write in this
margin

Answer $x = \dots\dots\dots$ or $\dots\dots\dots$ [3]



Do not
write in this
margin

The diagram shows four points, A , B , P and Q , at sea.
 B is due South of A and P is due East of A .
 $AP = 3.73$ km, $BP = 5.47$ km, $AQ = 5.32$ km and $\angle PAQ = 25^\circ$.

(a) Calculate $\angle ABP$.

Answer [2]

(b) Calculate PQ .

Answer km [4]

(c) A boat sailed in a straight line from Q to A .

(i) Find the bearing of A from Q .

*Do not
write in this
margin*

Answer [1]

(ii) A lighthouse is situated at A .

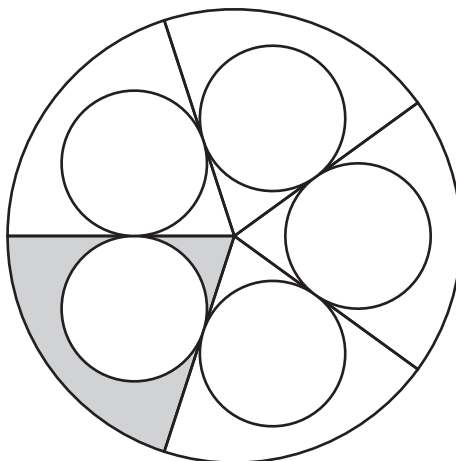
The top of the lighthouse is 30 m above sea level.

Calculate the angle of depression of the boat from the top of the lighthouse when the boat is 100 m from A .

Answer [2]

3 (a)

Diagram I



Do not
write in this
margin

Diagram I shows one large circle and five identical small circles.
Each of the five radii shown is a tangent to two of the small circles.

- (i) Describe the symmetry of the diagram.

Answer [1]

- (ii) The radius of the large circle is R centimetres and the radius of each small circle is r centimetres.
Each small circle is equal in area to the shaded region.

Find $R^2 : r^2$.

Answer : [3]

(b)

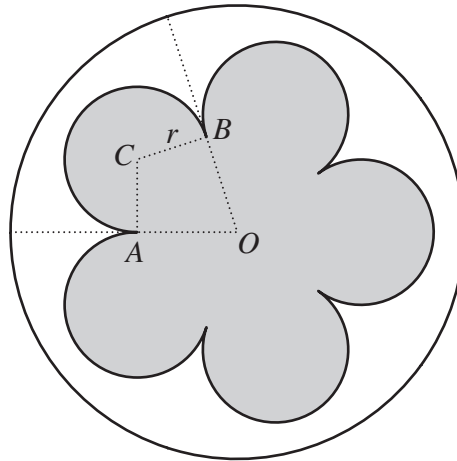
 Do not
 write in this
 margin
Diagram II

Diagram II shows the same large circle and arcs of the same small circles as in **Diagram I**. C is the centre of one of the small circles.

This circle touches the adjacent circles at A and B .

O is the centre of the large circle.

- (i) Show that reflex $\hat{ACB} = 252^\circ$.

[2]

- (ii) The perimeter of the shaded region is $k\pi r$ centimetres.

Calculate the value of k .

Answer [2]

- 4 (a) A shopkeeper buys some plates from a manufacturer for \$10 each.

- (i) (a) The shopkeeper sells a plate for \$12.

Calculate the percentage profit.

Answer% [1]

- (b) The shopkeeper buys 240 plates and sells 180 at \$12 each.
The rest were sold to a café for a total of \$540.

Calculate the percentage discount given to the café.

Answer% [2]

- (ii) The manufacturer made a profit of 60% when he sold each plate for \$10.

Calculate the cost of manufacturing each plate.

Answer \$..... [2]

Do not
write in this
margin

- (b) Another shopkeeper bought 100 pans at \$5 each.
 He sold 63 at \$6 each and x at \$4 each.
 He did not sell all the pans nor enough to make an overall profit.

(i) Form an inequality in x .

Answer [1]

(ii) Hence find the greatest possible number of pans that were sold.

Answer [2]

- (c) One day, the rate of exchange between American dollars (\$) and British pounds (£) was $\$1.45 = \pounds 1$.

(i) Alan changed £300 into dollars.

Calculate how many dollars he received.

Answer \$..... [1]

(ii) On the same day, the rate of exchange between South African rands (R) and pounds was $\text{R}10.44 = \pounds 1$.

Calculate the number of rands received in exchange for one dollar.

Answer R..... [2]

5 (a) $\begin{pmatrix} 3 & -1 & 0 \\ 1 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ 11 \\ y \end{pmatrix} = \begin{pmatrix} 4 \\ 9 \end{pmatrix}.$

Find x and y .

Do not
write in this
margin

Answer $x = \dots\dots\dots$

$y = \dots\dots\dots$ [2]

(b) (i) The transformation A is represented by the matrix $\begin{pmatrix} a & b \\ c & d \end{pmatrix}.$

Find, in terms of a , b , c and d as appropriate,

(a) the image of $(1, 0)$ under the transformation A,

Answer $(\dots\dots\dots, \dots\dots\dots)$ [1]

(b) the image of $(0, 1)$ under the transformation A.

Answer $(\dots\dots\dots, \dots\dots\dots)$ [1]

- (ii) The transformation B maps (1, 0) onto (1, 3) and (0, 1) onto (−3, −2).

Write down the matrix that represents transformation B.

*Do not
write in this
margin*

Answer $\begin{pmatrix} & \\ & \end{pmatrix}$ [1]

- (iii) Describe fully the transformation given by the matrix $\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$.

Answer
 [2]

- 6 You may use the graph paper on the next page to help answer this question.

The point A is $(0, 7)$, and the point B is $(6, 9)$.

- (a) Express $\overrightarrow{AB}$ as a column vector.

Answer [1]

- (b) Find the gradient of AB .

Answer [1]

- (c) The equation of the line AB is $x + Py + Q = 0$.

Find P and Q .

Answer $P =$
 $Q =$ [2]

- (d) The point C is $(12, 2)$.

- (i) Given that C is the midpoint of BM , find the coordinates of M .

Answer (.....,) [1]

- (ii) Calculate AC .

Answer units [1]

Do not
write in this
margin

- (iii) The point D lies on the line AB .
 The line CD is parallel to the y -axis.

(a) Find the coordinates of D .

Answer (.....,) [2]

(b) Express $\overrightarrow{AD}$ in terms of $\overrightarrow{AB}$.

Answer $\overrightarrow{AD} = \dots\dots\dots$ [1]

Do not
write in this
margin



Section B [48 marks]

Answer **four** questions in this section.

Each question in this section carries 12 marks.

Do not
write in this
margin

7

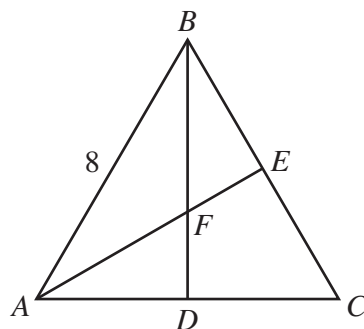


Diagram I

In **Diagram I**, ABC is an equilateral triangle of side 8 cm.
 D and E are the midpoints of AC and BC respectively.
 BD and AE intersect at F .

- (a) (i) Find the area of triangle ABC .

Answercm² [2]

- (ii) Show that $\angle AFB = 120^\circ$.

Answer
..... [1]

- (iii) Calculate AF .

Answercm [2]

- (b) [The volume of a pyramid = $\frac{1}{3} \times \text{base area} \times \text{height}$]

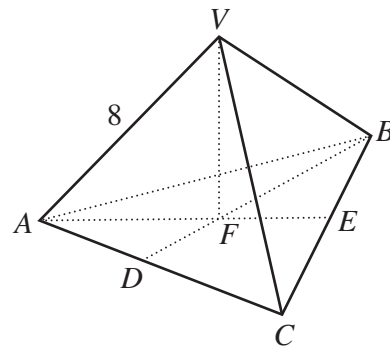


Diagram II

The equilateral triangle of side 8 cm in **Diagram I** forms the base of the triangular pyramid $VABC$ in **Diagram II**.

The vertex V is vertically above F .

$VA = VB = VC = 8$ cm.

- (i) Calculate the surface area of the pyramid.

Answercm² [1]

- (ii) Calculate the volume of the pyramid.

Answercm³ [3]

- (c) A pyramid P is geometrically similar to $VABC$ and its volume is $\frac{1}{64}$ of the volume of $VABC$.

- (i) Find the length of an edge of P .

Answer cm [2]

- (ii) A pyramid that is identical to P is removed from each of the four vertices of $VABC$.

State the number of faces of the new solid.

Answer [1]

Do not
write in this
margin

- 8 Two companies, A and B, were started 10 years ago.
Initial investments of \$25 or multiples of \$25 could be made when Company A started business.

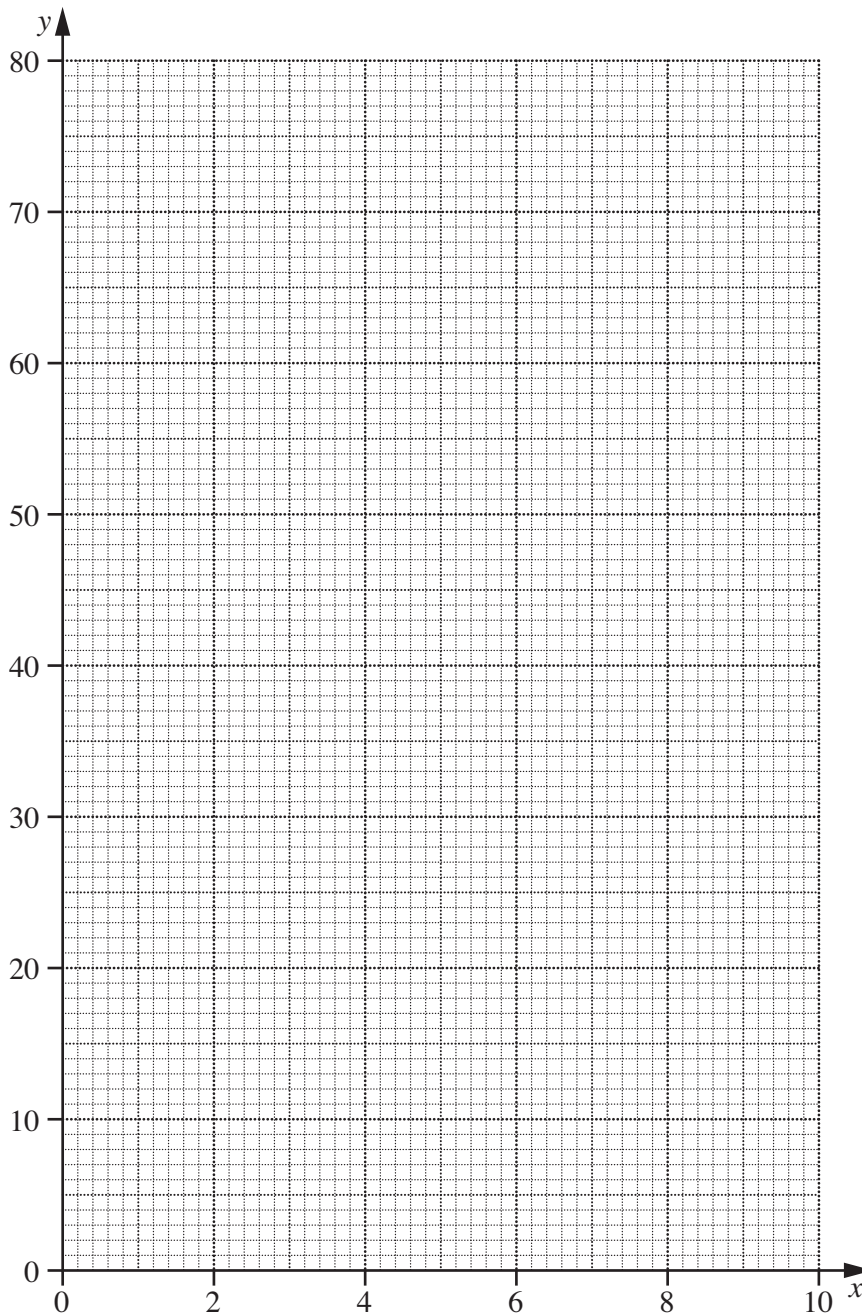
(a) The table shows the value of an initial investment of \$25 at the end of each of the next 10 years.

Number of years (x)	0	1	2	3	4	5	6	7	8	9	10
Value in dollars (y)	25	28	31	35	39	44	49	55	62	69	78

- (i) Calculate the value of an initial investment of \$500 after 8 years.

Answer \$..... [1]

- (ii) On the grid, plot the points given in the table and join them with a smooth curve.



[2]

- (iii) Using your graph, find x when the value of an initial investment of \$100 had increased to \$168.

Answer [1]

- (b) An initial investment of \$25 was made when company B started business. The value, y dollars, after x years, is given by the equation $y = 3.75x + 25$.

- (i) Calculate the value of an initial investment of \$500 after 8 years.

Answer \$..... [1]

- (ii) On the grid, draw the graph of $y = 3.75x + 25$. [2]

- (c) Using your graphs, find the value of x when an initial investment of \$25 had increased to the same value in each company.

Answer [1]

- (d) (i) By drawing a tangent to the graph representing an investment in company A, find the rate of increase of this investment when $x = 7$.

Answer [2]

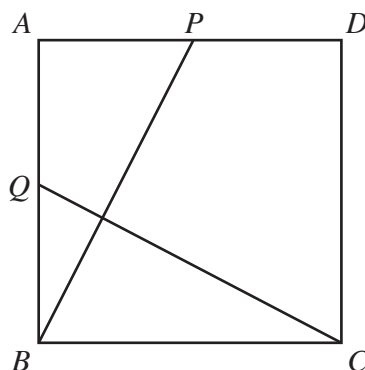
- (ii) **State** the rate of increase of an investment in company B.

Answer [1]

- (iii) By drawing another tangent to the graph representing an investment in company A, find the value of x when the rates of increase of investments in each company were the same.

Answer [1]

Diagram I



In **Diagram I**, $ABCD$ is a square.
 P and Q are the midpoints of AD and AB respectively.

(a) Show that triangles APB and BQC are congruent.

Answer

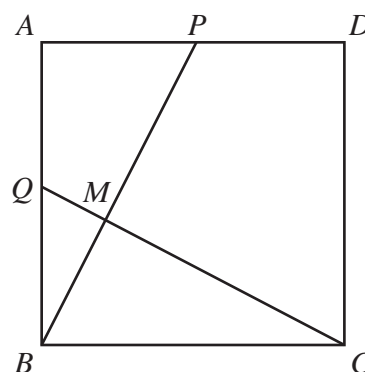
.....

.....

..... [3]

(b)

Diagram II



In **Diagram II**, QC and PB intersect at M .

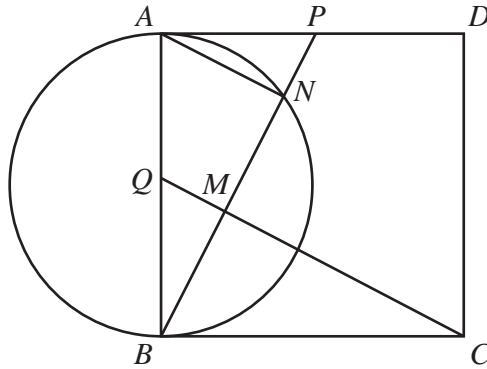
Show that $\angle BMC = 90^\circ$.
State your reasons clearly.

Answer

.....

..... [2]

(c)

Diagram III

Do not
write in this
margin

In **Diagram III**, the circle centre Q has diameter AB .
 The circle intersects BP at N .

- (i) State the reason why $\angle ANB = 90^\circ$.

Answer [1]

- (ii) Triangle BMQ is mapped onto triangle BNA by an enlargement.
 Write down the centre and scale factor of the enlargement.

Answer [1]

- (iii) Given that $QM = 3$ cm,

- (a) find AN ,

Answer cm [1]

- (b) show that $MN = 6$ cm,

Answer [1]

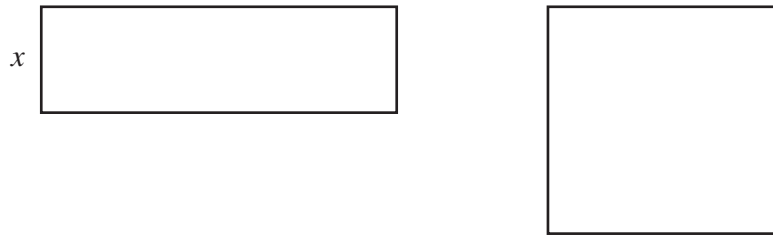
- (c) find MC ,

Answer cm [1]

- (d) find the area of triangle APB .

Answer cm² [2]

10


 Do not
 write in this
 margin

A piece of wire, 28 cm in length, is cut into two parts.
 One part is used to make a rectangle and the other a square.

The length of the rectangle is three times its width.
 The width of the rectangle is x centimetres.

- (a) (i) Write down an expression, in terms of x , for the length of the rectangle.

Answer cm [1]

- (ii) Find, and simplify, an expression, in terms of x , for the length of a side of the square.

Answer cm [2]

- (b) It is given that the area of the rectangle is equal to the area of the square.

- (i) Form an equation in x and show that it reduces to $x^2 - 28x + 49 = 0$.

[2]

- (ii) Solve the equation $x^2 - 28x + 49 = 0$, giving each solution correct to 3 significant figures.

*Do not
write in this
margin*

Answer $x = \dots\dots\dots$ or $\dots\dots\dots$ [4]

- (iii) Which solution represents the width of the rectangle?
Give a reason for your answer.

Answer The width of the rectangle is $\dots\dots\dots$ cm because $\dots\dots\dots$
 $\dots\dots\dots$ [2]

- (iv) Calculate the area of the square.

Answer $\dots\dots\dots$ cm² [1]

- 11 (a)** A sports club has 120 members.
 The cumulative frequency table for their ages is shown below.

*Do not
 write in this
 margin*

Age (x years)	$x \leq 5$	$x \leq 15$	$x \leq 25$	$x \leq 35$	$x \leq 45$	$x \leq 55$	$x \leq 65$
Cumulative frequency	0	12	30	60	96	114	120

- (i)** On the grid on the next page
 draw a horizontal x -axis for $0 \leq x \leq 70$, using a scale of 2 cm to represent 10 years
 and a vertical axis from 0 to 120, using a scale of 2 cm to represent 20 members.

On your axes draw a smooth cumulative frequency curve to illustrate the information
 in the table. [3]

- (ii)** Find the upper quartile age.

Answeryears [1]

- (iii)** Find the interquartile range of the ages.

Answeryears [1]

- (iv)** Members who are not more than 15, and members who are over 50, pay reduced fees.
 Use your graph to find an estimate of the number of members who pay reduced fees.

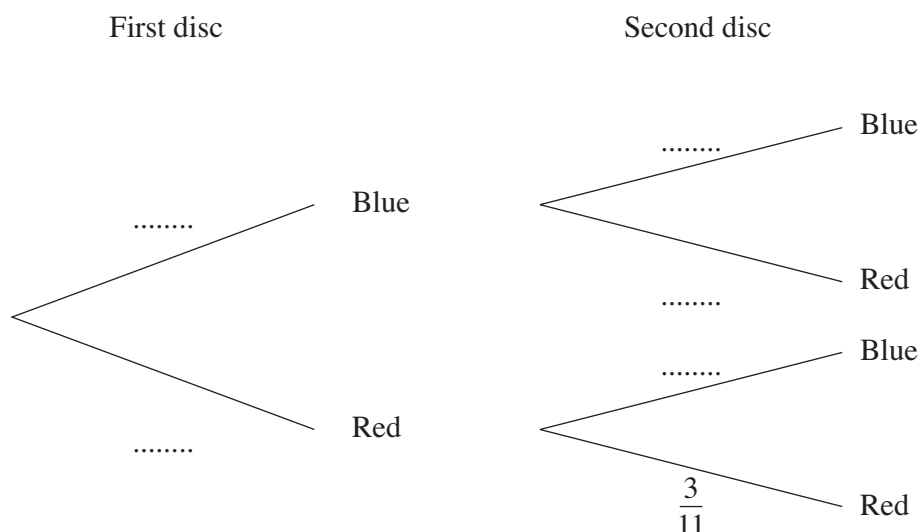
Answer [1]

*Do not
write in this
margin*



Turn over for the rest of this question.

The tree diagram below shows the possible outcomes and one of their probabilities.



- (i) Complete the tree diagram. [2]

- (ii) Expressing each of your answers as a fraction **in its lowest terms**, calculate the probability that

- (a)** both discs are red,

Answer [1]

- (b)** at least one disc is blue.

Answer [2]

- (iii) A third disc is picked out at random.
Calculate the probability that all three discs are red.

Answer [1]

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

University of Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.