CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

MARK SCHEME for the October/November 2012 series

9709 MATHEMATICS

9709/32 Paper 3, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2012 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.





Page 2	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2012	9709	32

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.



Page 3	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2012	9709	32

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.



Page 4	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2012	9709	32

- State or imply non-modular inequality $(3(x-1))^2 < (2x+1)^2$ 1 **EITHER**
 - or corresponding quadratic equation, or pair of linear equations $3(x-1) = \pm (2x+1)$ **B**1
 - Make reasonable solution attempt at a 3-term quadratic, or solve two linear
 - equations M1
 - Obtain critical values $x = \frac{2}{5}$ and x = 4**A**1
 - State answer $\frac{2}{5} < x < 4$ **A**1
 - Obtain critical value $x = \frac{2}{5}$ or x = 4 from a graphical method, or by inspection, or by OR
 - solving a linear equation or inequality B1
 - Obtain critical values $x = \frac{2}{5}$ and x = 4B₂
 - State answer $\frac{2}{5} < x < 4$ B1 [4]

[Do not condone \leq for <.]

- Use laws of indices correctly and solve for 5^x or for 5^{-x} or for 5^{x-1} 2 **EITHER** M1
 - Obtain 5^x or for 5^{-x} or for 5^{x-1} in any correct form, e.g. $5^x = \frac{5}{1-\frac{1}{5}}$ **A**1
 - Use correct method for solving $5^x = a$, or $5^{-x} = a$, or $5^{x-1} = a$, where a > 0M1
 - Obtain answer x = 1.14**A**1
 - Use an appropriate iterative formula, e.g. $x_{n+1} = \frac{\ln(5^{x-1}+5)}{\ln 5}$, correctly, at least once ORM1
 - Obtain answer 1.14 **A**1
 - Show sufficient iterations to at least 3 d.p. to justify 1.14 to 2 d.p., or show there is a sign change in the interval (1.135, 1.145)
 - **A**1 Show there is no other root **A**1 [4]
 - [For the solution x = 1.14 with no relevant working give B1, and a further B1 if 1.14 is shown to be the only solution.]
- 3 Attempt use of $\sin (A + B)$ and $\cos (A - B)$ formulate to obtain an equation in $\cos \theta$ and $\sin \theta$ M1
 - Obtain a correct equation in any form **A**1
 - Use trig. formula to obtain an equation in $\tan \theta$ (or $\cos \theta$, $\sin \theta$ or $\cot \theta$) M1
 - Obtain tan $\theta = \frac{\sqrt{6} 1}{1 \sqrt{2}}$, or equivalent (or find cost θ , sin θ or cot θ) A₁
 - Obtain answer $\theta = 105.9^{\circ}$, and no others in the given interval A₁ [5]
 - [Ignore answers outside the given material]
- 4 Obtain correct unsimplified terms in x and x^3 B1 + B1Equate coefficients and solve for a M1
 - Obtain final answer $a = \frac{1}{\sqrt{2}}$, or exact equivalent A₁ [4]
 - (ii) Use correct method and value of a to find the first two terms of the expansion $(1 + ax)^{-2}$ A1 √ Obtain $1 - \sqrt{2x}$, or equivalent
 - Obtain term $\frac{3}{2}x^2$ A1 √ [3]
 - [Symbolic coefficients, e.g. $\binom{-2}{1}a$, are not sufficient for the first B marks] [The f.t. is solely on the value of a.]



Page 5	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2012	9709	32

- 5 (i) Use correct quotient or chain rule

 Obtain the given answer correctly having shown sufficient working

 A1 [7]
 - Obtain the given answer correctly having shown sufficient working

 A1 [2]
 - (ii) Use a valid method, e.g. multiply numerator and denominator by $\sec x + \tan x$, and a version of Pythagoras to justify the given identity

 B1 [1]
 - (iii) Substitute, expand $(\sec x + \tan x)^2$ and use Pythagoras once
 Obtain given identity

 M1
 [2]
 - (iv) Obtain integral $2 \tan x x + 2 \sec x$ B1

 Use correct limits correctly in an expression of the form $a \tan x + bx + c \sec x$, or equivalent, where $abc \neq 0$ M1

 Obtain the given answer correctly A1 [3]
- 6 Separate variables correctly and attempt integration of one side
 Obtain term ln x

 B1
 - State or imply $\frac{1}{1-y^2} \equiv \frac{A}{1-y} + \frac{B}{1+y}$ and use a relevant method to find A or B

Obtain $A = \frac{1}{2}$, $B = \frac{1}{2}$

Integrate and obtain $-\frac{1}{2} \ln (1-y) + \frac{1}{2} \ln (1+y)$, or equivalent

[If the integral is directly stated as $k_1 \ln\left(\frac{1+y}{1-y}\right)$ or $k_2 \ln\left(\frac{1-y}{1+y}\right)$ give M1, and then A2 for $k_1 = \frac{1}{2}$ or $k_2 = -\frac{1}{2}$]

Evaluate a constant, or use limits x = 2, y = 0 in a solution containing terms $a \ln x$, $b \ln (1 - y)$ and $c \ln (1 + y)$ where $abc \neq 0$

and $c \ln (1 + y)$, where $abc \neq 0$ M1 [This M mark is not available if the integral of $1/(1 - y^2)$ is initially taken to be of the form $k \ln (1 - y^2)$]

Obtain solution in any correct form, e.g. $\frac{1}{2} \ln \left(\frac{1+y}{1-y} \right) = \ln x - \ln 2$

Rearrange and obtain $y = \frac{x^2 - 4}{x^2 + 4}$, or equivalent, free of logarithms

A1 [8]

7 (i) EITHER: State or imply $\frac{1}{x} + \frac{1}{y} \frac{dy}{dx}$ as derivative of $\ln xy$, or equivalent B1

State or imply $3y^2 \frac{dy}{dx}$ as derivative of y^3 , or equivalent B1

Equate derivative of LHS to zero and solve for $\frac{dy}{dx}$ M1

Obtain the given answer

OR
Obtain $xy = \exp(1 + y^3)$ and state or imply $y + x \frac{dy}{dx}$ as derivative of xyB1

State or imply $3y^2 \frac{dy}{dx} \exp(1+y^3)$ as derivative of $(1+y^3)$

Equate derivatives and solve for $\frac{dy}{dx}$ M1

Obtain the given answer

A1 [4]

[The M1 is dependent on at least one of the B marks being earned]

(ii) Equate denominator to zero and solve for y M1*
Obtain y = 0.693 only
Substitute found value in the equation and solve for y M1(d)

Substitute found value in the equation and solve for x M1(dep*) Obtain x = 5.47 only

GCE AS/A LEVEL – October/November 2012 9709 32	Page 6	Mark Scheme	Syllabus	Paper
		GCE AS/A LEVEL – October/November 2012	9709	

- 8 (i) Use correct product or quotient rule and use chain rule at least once
 Obtain derivative in any correct form
 Equate derivative to zero and solve an equation with at least two non-zero terms
 for real xObtain answer $x = \frac{1}{\sqrt{2}}$, or exact equivalent

 A1 [4]
 - (ii) State a suitable equation, e.g. $\alpha = \sqrt{(\ln(4 + 8\alpha^2))}$ B1

 Rearrange to reach $e^{\alpha^2} = 4 + 8\alpha^2$ B1

 Obtain $\frac{1}{2} = e^{-\frac{1}{2}\alpha^2} \sqrt{(1 + 2\alpha^2)}$, or work *vice versa* B1 [3]
 - (iii) Use the iterative formula correctly at least once
 Obtain final answer 1.86
 Show sufficient iterations to 4 d.p. to justify 1.86 to 2 d.p., or show there is a sign change in the interval (1.855, 1.865)

 A1
 [3]
- Substitute $x = 1 + \sqrt{2}$ i and attempt the expansions of the x^2 and x^4 terms *EITHER* M1 Use $i^2 = -1$ correctly at least once **B**1 Complete the verification **A**1 State second root $1 - \sqrt{2}i$ **B**1 OR 1 State second root $1 - \sqrt{2}i$ **B**1 Carry out a complete method for finding a quadratic factor with zeros $1 \pm \sqrt{2}$ i M1 Obtain $x^2 - 2x + 3$, or equivalent A1 Show that the division of p(x) by $x^2 - 2x + 3$ gives zero remainder and complete the verification A1 Substitute $x = 1 + \sqrt{2}$ i and use correct method to express x^2 and x^4 in polar form M1 OR 2 Obtain x^2 and x^4 in any correct polar form (allow decimals here) B1 Complete an exact verification A₁ State second root $1 - \sqrt{2}$ i, or its polar equivalent (allow decimals here) [4] B1

[The second M1 is earned if inspection reaches an unknown factor $x^2 + Bx + C$ and an equation in B and/or C, or an unknown factor $Ax^2 + Bx + (6/3)$ and an equation in A and/or B] [If part (i) is attempted by the OR 1 method, then an attempt at part (ii) which uses or quotes relevant working or results obtained in part (i) should be marked using the scheme for part (ii)]



Page 7	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2012	9709	32

equations in a,b,c , e.g. $a-5b-3c=0$ and $a-b-3c=0$ State two correct equations in a,b,c Solve simultaneous equations and find one ratio, e.g. $a:c$, or $b=0$ Obtain $a:b:c=3:0:1$, or equivalent Substitute a relevant point in $3x+z=d$ and evaluate d Obtain equation $3x+z=13$, or equivalent OR 1 Attempt to calculate vector product of relevant vectors, e.g. $(\mathbf{i}-5\mathbf{j}-3\mathbf{k})\times(\mathbf{i}-\mathbf{j}-3\mathbf{k})$ Obtain 2 correct components of the product Obtain correct product, e.g. $12\mathbf{i}+4\mathbf{k}$ Substitute a relevant point in $12x+4z=d$ and evaluate d Obtain $3x+z=13$, or equivalent OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r}=3\mathbf{i}-2\mathbf{j}+4\mathbf{k}+\lambda(\mathbf{i}-5\mathbf{j}-3\mathbf{k})+\mu(\mathbf{i}-\mathbf{j}-3\mathbf{k})$ A1 State 3 equations in x, y, z, λ and μ Eliminate λ and μ Obtain equation $3x+z=13$, or equivalent A1 [6]	10 (i)	EITHER	Use scalar product of relevant vectors, or subtract point equations to form two	
Solve simultaneous equations and find one ratio, e.g. $a:c$, or $b=0$ Obtain $a:b:c=3:0:1$, or equivalent Substitute a relevant point in $3x+z=d$ and evaluate d Obtain equation $3x+z=13$, or equivalent OR 1 Attempt to calculate vector product of relevant vectors, e.g. $(\mathbf{i}-5\mathbf{j}-3\mathbf{k})\times(\mathbf{i}-\mathbf{j}-3\mathbf{k})$ Obtain 2 correct components of the product Obtain correct product, e.g. $12\mathbf{i}+4\mathbf{k}$ Substitute a relevant point in $12x+4z=d$ and evaluate d Obtain $3x+z=13$, or equivalent OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r}=3\mathbf{i}-2\mathbf{j}+4\mathbf{k}+\lambda(\mathbf{i}-5\mathbf{j}-3\mathbf{k})+\mu(\mathbf{i}-\mathbf{j}-3\mathbf{k})$ A1 State 3 equations in x, y, z, λ and μ Eliminate λ and μ Obtain equation $3x+z=13$, or equivalent A1 [6]	10 (1)	BITTIER		M1*
Obtain $a:b:c=3:0:1$, or equivalent Substitute a relevant point in $3x+z=d$ and evaluate d Obtain equation $3x+z=13$, or equivalent OR 1 Attempt to calculate vector product of relevant vectors, e.g. $(\mathbf{i}-5\mathbf{j}-3\mathbf{k}) \times (\mathbf{i}-\mathbf{j}-3\mathbf{k})$ Obtain 2 correct components of the product Obtain correct product, e.g. $12\mathbf{i}+4\mathbf{k}$ Substitute a relevant point in $12x+4z=d$ and evaluate d Obtain $3x+z=13$, or equivalent OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r}=3\mathbf{i}-2\mathbf{j}+4\mathbf{k}+\lambda(\mathbf{i}-5\mathbf{j}-3\mathbf{k})+\mu(\mathbf{i}-\mathbf{j}-3\mathbf{k})$ A1 State 3 equations in x, y, z, λ and μ Eliminate λ and μ Obtain equation $3x+z=13$, or equivalent A1 M1 (dep*) A1 A1 Eliminate λ and μ Obtain equation $3x+z=13$, or equivalent A1 [6]				A1
Substitute a relevant point in $3x + z = d$ and evaluate d Obtain equation $3x + z = 13$, or equivalent Attempt to calculate vector product of relevant vectors, e.g. $(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) \times (\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ Obtain 2 correct components of the product Obtain correct product, e.g. $12\mathbf{i} + 4\mathbf{k}$ Substitute a relevant point in $12x + 4z = d$ and evaluate d Obtain $3x + z = 13$, or equivalent OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ A1 State 3 equations in x , y , z , λ and μ Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent A1 M1 (dep*) A1				M1 (dep*)
Obtain equation $3x + z = 13$, or equivalent Attempt to calculate vector product of relevant vectors, e.g. $(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) \times (\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ Obtain 2 correct components of the product Obtain correct product, e.g. $12\mathbf{i} + 4\mathbf{k}$ Substitute a relevant point in $12x + 4z = d$ and evaluate d Obtain $3x + z = 13$, or equivalent OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ At Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent A1 M1 (dep*) A1 A1 A1 A1 A1 A1 A1 A1 A1 A				
Attempt to calculate vector product of relevant vectors, e.g. $(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) \times (\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ M2* Obtain 2 correct components of the product A1 Obtain correct product, e.g. $12\mathbf{i} + 4\mathbf{k}$ A1 Substitute a relevant point in $12x + 4z = d$ and evaluate d M1 (dep*) Obtain $3x + z = 13$, or equivalent A1 OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ A1 State 3 equations in x , y , z , λ and μ A1 Eliminate λ and μ M1 (dep*) Obtain equation $3x + z = 13$, or equivalent A1 [6]				
e.g. $(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) \times (\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ Obtain 2 correct components of the product Obtain correct product, e.g. $12\mathbf{i} + 4\mathbf{k}$ Substitute a relevant point in $12x + 4z = d$ and evaluate d Obtain $3x + z = 13$, or equivalent OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ A1 State 3 equations in x , y , z , λ and μ Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent M2* A1 M1 (dep*) A1 M1 (dep*) A1 [6]		OR 1	*	Al
Obtain 2 correct components of the product Obtain correct product, e.g. $12\mathbf{i} + 4\mathbf{k}$ Substitute a relevant point in $12x + 4z = d$ and evaluate d Obtain $3x + z = 13$, or equivalent OR 2 Attempt to form 2—parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ Al State 3 equations in x , y , z , λ and μ Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent Al M1 (dep*) Al M1 (dep*) Al Al Al Al Al Al Al Al Al A		OR I		M2*
Obtain correct product, e.g. $12\mathbf{i} + 4\mathbf{k}$ Substitute a relevant point in $12x + 4z = d$ and evaluate d Obtain $3x + z = 13$, or equivalent OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ A1 State 3 equations in x , y , z , λ and μ Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent A1 M1 (dep*) A1 M1 (dep*) A1 [6]			-	
Obtain $3x + z = 13$, or equivalent A1 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ A1 State 3 equations in x , y , z , λ and μ Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent A1 M1 (dep*) A1 [6]				
OR 2 Attempt to form 2-parameter equation for the plane with relevant vectors State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ A1 State 3 equations in x , y , z , λ and μ A1 Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent A1 [6]				M1 (dep*)
State a correct equation e.g. $\mathbf{r} = 3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 5\mathbf{j} - 3\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 3\mathbf{k})$ A1 State 3 equations in x , y , z , λ and μ A1 Eliminate λ and μ M1 (dep*) Obtain equation $3x + z = 13$, or equivalent A1 [6]			-	
State 3 equations in x , y , z , λ and μ Eliminate λ and μ Obtain equation $3x + z = 13$, or equivalent A1 [6]		OR 2		
Eliminate λ and μ M1 (dep*) Obtain equation $3x + z = 13$, or equivalent A1 [6]				
Obtain equation $3x + z = 13$, or equivalent A1 [6]				
			· ·	\ 1 /
\longrightarrow			Obtain equation $3x + 2 - 13$, of equivalent	Ai [0]
(ii) EITHER Find \overline{CP} for a point P on AB with a parameter t, e.g. $2\mathbf{i} + 3\mathbf{j} + 7\mathbf{k} + t(-\mathbf{i} + \mathbf{j} + 3\mathbf{k})$ B1 $\sqrt{}$	(ii)	EITHER	Find \overrightarrow{CP} for a point P on AB with a parameter t, e.g. $2\mathbf{i} + 3\mathbf{j} + 7\mathbf{k} + t(-\mathbf{i} + \mathbf{j} + 3\mathbf{k})$	B1 √
Either: Equate scalar product \overrightarrow{CP} , \overrightarrow{AB} to zero and form an equation in t	()			
Or 1: Equate derivative for \mathbb{CP}^2 (or \mathbb{CP}) to zero and form an equation in t				
Or 1. Equate derivative for CF (of CF) to zero and form an equation in t CF (or CPB) and form an equation in t CF CF CF CF CF CF CF CF				M1
Solve and obtain correct value of t , e.g. $t = -2$				
Carry out a complete method for finding the length of <i>CP</i> M1				
Obtain answer $3\sqrt{2}$ (4.24), or equivalent A1				A1
OR 1 State \overrightarrow{AC} (or \overrightarrow{BC}) and \overrightarrow{AB} in component form		OR 1		B1 √
Using a relevant scalar product find the cosine of CAB (or CBA) M1				M1
Obtain cost $CAB = -\frac{22}{\sqrt{11}\sqrt{62}}$, or cos $CBA = \frac{33}{\sqrt{11}\sqrt{117}}$, or equivalent			Obtain cost $CAB = -\frac{22}{\sqrt{11}\sqrt{62}}$, or cos $CBA = \frac{33}{\sqrt{11}\sqrt{117}}$, or equivalent	A1
Use trig to find the length of the perpendicular M1			V111V11/	M1
Obtain answer $3\sqrt{2}$ (4.24), or equivalent A1				A1
OR 2 State \overrightarrow{AC} (or \overrightarrow{BC}) and \overrightarrow{AB} in component form		OR 2		B1 √
Using a relevant scalar product find the length of the projection AC (or BC)				
on AB M1				M1
Obtain answer $2\sqrt{11}$ (or), $3\sqrt{11}$ or equivalent			Obtain answer $2\sqrt{11}$ (or), $3\sqrt{11}$ or equivalent	A1
Use Pythagoras to find the length of the perpendicular M1				M1
Obtain answer $3\sqrt{2}$ (4.24), or equivalent A1			Obtain answer $3\sqrt{2}$ (4.24), or equivalent	A1
OR 3 State \overrightarrow{AC} (or \overrightarrow{BC}) and \overrightarrow{AB} in component form		OR 3		B1 √
Calculate their vector product, e.g. $(-2\mathbf{i} - 3\mathbf{j} - 7\mathbf{k}) \times (-\mathbf{i} + \mathbf{j} + 3\mathbf{k})$ M1			Calculate their vector product, e.g. $(-2\mathbf{i} - 3\mathbf{j} - 7\mathbf{k}) \times (-\mathbf{i} + \mathbf{j} + 3\mathbf{k})$	M1
Obtain correct product, e.g. $-2\mathbf{i} + 13\mathbf{j} - 5\mathbf{k}$ A1				A1
Divide modulus of the product by the modulus of \overrightarrow{AB} M1			Divide modulus of the product by the modulus of \overrightarrow{AB}	M1
Obtain answer $3\sqrt{2}$ (4.24), or equivalent A1			Obtain answer $3\sqrt{2}$ (4.24), or equivalent	A1
OR 4 State two of \overrightarrow{AB} , \overrightarrow{BC}) and \overrightarrow{AC} in component form		OR 4	State two of \overrightarrow{AB} , \overrightarrow{BC}) and \overrightarrow{AC} in component form	B1 √
Use cosine formula in triangle ABC to find $\cos A$ or $\cos B$ M1				M1
Obtain $\cos A = -\frac{44}{2\sqrt{11}\sqrt{62}}$, or $\cos B = \frac{66}{2\sqrt{11}\sqrt{117}}$			Obtain $\cos A = -\frac{44}{2\sqrt{11}\sqrt{62}}$, or $\cos B = \frac{66}{2\sqrt{11}\sqrt{117}}$	A1
Use trig to find the length of the perpendicular M1				M1
Obtain answer $3\sqrt{2}$ (4.24), or equivalent A1 [5]			* * * *	A1 [5]
[The f.t is on \overrightarrow{AB}]				

