This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners’ meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

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Mark Scheme Notes

Marks are of the following three types:

M  Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A  Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B  Mark for a correct result or statement independent of method marks.

When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol $\checkmark$ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking $g$ equal to 9.8 or 9.81 instead of 10.
The following abbreviations may be used in a mark scheme or used on the scripts:

**AEF**  Any Equivalent Form (of answer is equally acceptable)

**AG**  Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

**BOD**  Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

**CAO**  Correct Answer Only (emphasising that no “follow through” from a previous error is allowed)

**CWO**  Correct Working Only – often written by a ‘fortuitous’ answer

**ISW**  Ignore Subsequent Working

**MR**  Misread

**PA**  Premature Approximation (resulting in basically correct work that is insufficiently accurate)

**SOS**  See Other Solution (the candidate makes a better attempt at the same question)

**SR**  Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

### Penalties

**MR –1**  A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through” marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

**PA –1**  This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.
1 **EITHER:** State or imply non-modular inequality \((2x - 5)^2 > (3(2x + 1))^2\), or corresponding quadratic equation, or pair of linear equations \((2x - 5) = \pm 3(2x + 1)\) B1
Make reasonable solution attempt at a 3-term quadratic, or solve two linear equations for \(x\) M1
Obtain critical values \(-2\) and \(\frac{1}{4}\) A1
State final answer \(-2 < x < \frac{1}{4}\) A1

**OR:** Obtain critical value \(x = -2\) from a graphical method, or by inspection, or by solving a linear equation or inequality B1
Obtain critical value \(x = \frac{1}{4}\) similarly B2
State final answer \(-2 < x < \frac{1}{4}\) B1 [4]
[Do not condone \(\leq\) for < ]

2 State or imply \(1 + u = u^2\) B1
Solve for \(u\) M1
Obtain root \(\frac{1}{2}(1 + \sqrt{5})\), or decimal in \([1.61, 1.62]\) A1
Use correct method for finding \(x\) from a positive root M1
Obtain \(x = 0.438\) and no other answer A1 [5]

3 Use \(\tan(A \pm B)\) and obtain an equation in \(\tan \theta\) and \(\tan \phi\) M1*
Substitute throughout for \(\tan \theta\) or for \(\tan \phi\) dep M1*
Obtain \(3\tan^2 \theta - \tan \theta - 4 = 0\) or \(3\tan^2 \phi - 5\tan \phi - 2 = 0\), or 3-term equivalent A1
Solve a 3-term quadratic and find an angle M1
Obtain answer \(\theta = 135^\circ\), \(\phi = 63.4^\circ\) A1
Obtain answer \(\theta = 53.1^\circ\), \(\phi = 161.6^\circ\) A1 [6]
[Treat answers in radians as a misread. Ignore answers outside the given interval.]
[SR: Two correct values of \(\theta\) (or \(\phi\)) score A1; then A1 for both correct \(\theta\), \(\phi\) pairs.]

4 (i) Evaluate, or consider the sign of, \(x^3 - x^2 - 6\) for two integer values of \(x\), or equivalent M1
Obtain the pair \(x = 2\) and \(x = 3\), with no errors seen A1 [2]

(ii) State a suitable equation, e.g. \(x = \sqrt{(x + (6/x))}\) B1
Rearrange this as \(x^3 - x^2 - 6 = 0\), or work vice versa B1 [2]

(iii) Use the iterative formula correctly at least once M1
Obtain final answer 2.219 A1
Show sufficient iterates to 5 d.p. to justify 2.219 to 3 d.p., or show there is a sign change in the interval \((2.2185, 2.2195)\) A1 [3]
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<td>5</td>
<td>(i) State or imply that the derivative of $e^{-2x}$ is $-2e^{-2x}$</td>
<td>B1</td>
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<td></td>
<td>Use product or quotient rule</td>
<td>M1</td>
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<td>Obtain correct derivative in any form</td>
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<td>Use Pythagoras</td>
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<td>(ii)</td>
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<td>B1</td>
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<td>(iii)</td>
<td>State answer $x = \frac{1}{4}\pi$</td>
<td>B1</td>
<td>[1]</td>
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<td>6</td>
<td>(i) Substitute $x = -1$, equate to zero and simplify at least as far as $-8 + a - b - 1 = 0$</td>
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<td></td>
<td>Substitute $x = -\frac{1}{2}$ and equate the result to 1</td>
<td>M1</td>
<td></td>
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<tr>
<td></td>
<td>Obtain a correct equation in any form, e.g. $-1 + \frac{1}{4}a - \frac{1}{2}b - 1 = 1$</td>
<td>A1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Solve for $a$ or for $b$</td>
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<td></td>
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<tr>
<td></td>
<td>Obtain $a = 6$ and $b = -3$</td>
<td>A1</td>
<td>[5]</td>
</tr>
<tr>
<td>(ii)</td>
<td>Commence division by $(x + 1)$ reaching a partial quotient $8x^2 + kx$</td>
<td>M1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Obtain quadratic factor $8x^2 - 2x - 1$</td>
<td>A1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Obtain factorisation $(x + 1)(4x + 1)(2x - 1)$</td>
<td>A1</td>
<td>[3]</td>
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</table>
|   | [The M1 is earned if inspection reaches an unknown factor $8x^2 + Bx + C$ and an equation in $B$ and/or $C$, or an unknown factor $Ax^2 + Bx - 1$ and an equation in $A$ and/or $B$.]
|   | [If linear factors are found by the factor theorem, give B1B1 for $(2x - 1)$ and $(4x + 1)$, and B1 for the complete factorisation.]
| 7 | (i) Use correct method to form a vector equation for $AB$ | M1 | |
|   | Obtain a correct equation, e.g. $\mathbf{r} = i + 2j + \lambda(2i - 2j + k)$ or $\mathbf{r} = 3i + k + \mu(2i - 2j + k)$ | A1 | [2] |
| (ii) | Using a direction vector for $AB$ and a relevant point, obtain an equation for $m$ in any form | M1 | |
|   | Obtain answer $2x - 2y + z = 4$, or equivalent | A1 | [2] |
| (iii) | Express general point of $AB$ in component form, e.g. $(1 + 2\lambda, 2 - 2\lambda, \lambda)$ or $(3 + 2\mu, -2\mu, 1 + \mu)$ | B1 | |
|   | Substitute in equation of $m$ and solve for $\lambda$ or for $\mu$ | M1 | |
|   | Obtain final answer $\frac{7}{3}i + \frac{2}{3}j + \frac{2}{3}k$ for the position vector of $N$, from $\lambda = \frac{2}{3}$ or $\mu = -\frac{1}{3}$ | A1 | |
|   | Carry out a correct method for finding $CN$ | M1 | |
|   | Obtain the given answer $\sqrt{13}$ | A1 | [5] |
|   | [The f.t. is on the direction vector for $AB$.] | |
8 Separate variables and integrate one side 

Obtain term \( \ln(x + 2) \)

Use \( \cos 2A \) formula to express \( \sin^2 2\theta \) in the form \( a + b \cos 4\theta \)

Obtain correct form \( (1 - \cos 4\theta)/2 \), or equivalent

Integrate and obtain term \( \frac{1}{2} \theta - \frac{1}{8} \sin 4\theta \), or equivalent

Evaluate a constant, or use \( \theta = 0, x = 0 \) as limits in a solution containing terms 
\( c \ln(x + 2), d \sin(4\theta), e\theta \)

Obtain correct solution in any form, e.g. \( 2 \ln \left( \frac{4}{\sin \theta \left( \frac{1}{2} - \frac{1}{8} \sin 4\theta \right) + \ln 2} \right) \)

Obtain answer \( x = 0.962 \)

[9]

9 (i) Show \( u \) in a relatively correct position 

Show \( u^* \) in a relatively correct position

Show \( u^* - u \) in a relatively correct position

State or imply that \( OABC \) is a parallelogram

(ii) EITHER: Substitute for \( u \) and multiply numerator and denominator by \( 3 + i \), or equivalent

Simplify the numerator to \( 8 + 6i \) or the denominator to 10

Obtain final answer \( \frac{4}{5} + \frac{3}{5} i \), or equivalent

OR: Substitute for \( u \), obtain two equations in \( x \) and \( y \) and solve for \( x \) or for \( y \)

Obtain \( x = \frac{4}{5} \) or \( y = \frac{3}{5} \), or equivalent

Obtain final answer \( \frac{4}{5} + \frac{3}{5} i \), or equivalent

(iii) State or imply \( \arg(u^*/u) = \tan^{-1}\left(\frac{3}{4}\right) \)

Substitute exact arguments in \( \arg(u^*/u) = \arg u^* - \arg u \)

Fully justify the given statement using exact values

[3]

10 (i) Use the quotient rule

Obtain correct derivative in any form

Equate derivative to zero and solve for \( x \)

Obtain answer \( x = \frac{1}{\sqrt{2}} \), or exact equivalent

(ii) State or imply indefinite integral is of the form \( k \ln(1 + x^3) \)

State indefinite integral \( \frac{1}{3} \ln(1 + x^3) \)

State or imply limits correctly in an integral of the form \( k \ln(1 + x^3) \)

State or imply that the area of \( R \) is equal to \( \frac{1}{3} \ln(1 + p^3) - \frac{1}{3} \ln 2 \), or equivalent

Use a correct method for finding \( p \) from an equation of the form \( \ln(1 + p^3) = a \)

or \( \ln((1 + p^3)/2) = b \)

Obtain answer \( p = 3.40 \)

[2]