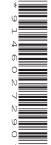


## Cambridge IGCSE<sup>™</sup>

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		



MATHEMATICS 0580/31

Paper 3 (Core) May/June 2020

2 hours

You must answer on the question paper.

You will need: Geometrical instruments

## **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For  $\pi$ , use either your calculator value or 3.142.

## **INFORMATION**

- The total mark for this paper is 104.
- The number of marks for each question or part question is shown in brackets [ ].

This document has 20 pages. Blank pages are indicated.

DC (LK/CB) 186453/2 © UCLES 2020

[Turn over

<ul><li>(ii) Show that the total number of seats is 380.</li><li>(b) Write down and simplify the ratio of the number of seats in each section A: B: C.</li></ul>		oriela designs the seating layout for a new theatre. re are three sections of seats, A, B and C.	
Section C has $\frac{3}{8}$ of the number of seats in Section A.  (i) Show that the number of seats in Section B is 171.  [ii) Show that the total number of seats is 380.  [iii) Show that the total number of seats is 380.  [iv) Write down and simplify the ratio of the number of seats in each section A: B: C.  A: B: C =	(a)		
<ul> <li>(i) Show that the number of seats in Section B is 171.</li> <li>(ii) Show that the total number of seats is 380.</li> <li>(b) Write down and simplify the ratio of the number of seats in each section A: B: C.</li> <li>A: B: C =</li></ul>			ı A.
<ul> <li>(ii) Show that the total number of seats is 380.</li> <li>(b) Write down and simplify the ratio of the number of seats in each section A: B: C.</li> <li>A: B: C =</li></ul>		Ç .	
<ul> <li>(b) Write down and simplify the ratio of the number of seats in each section A: B: C.</li> <li>A: B: C =</li></ul>		(ii) Show that the total number of seats is 380.	[1]
<ul> <li>(b) Write down and simplify the ratio of the number of seats in each section A: B: C.</li> <li>A: B: C =</li></ul>			
<ul> <li>(c) In Section A:</li> <li>There are 12 seats in the front row.</li> <li>Each row has 2 more seats than the row in front of it.</li> </ul>	(b)	Write down and simplify the ratio of the number of	of seats in each section A : B : C.
<ul> <li>(c) In Section A:</li> <li>There are 12 seats in the front row.</li> <li>Each row has 2 more seats than the row in front of it.</li> </ul>			
<ul> <li>There are 12 seats in the front row.</li> <li>Each row has 2 more seats than the row in front of it.</li> </ul>			A:B:C=:[2]
• Each row has 2 more seats than the row in front of it.	(c)	In Section A:	
		• There are 12 seats in the front row.	
Work out the number of rows for the 152 seats in Section A.		• Each row has 2 more seats than the row in	n front of it.
		Work out the number of rows for the 152 seats in	Section A.
			rows [2]

				3	
(d)	For	a concert in the the	atre, the ticke	et prices are in the ratio	
			A	: B : C = 9 : 7 : 4.	
	A ti	cket for Section C c	costs \$6.		
	(i)	Show that a ticket	for Section E	3 costs \$10.50.	
					[1]
(	ii)	Find the cost of a t	ticket for Sec	tion A.	
				\$	 [1]
(i	iii)	The table shows the	ne number of	\$ tickets sold in each section.	[1]
(i	iii)	The table shows th	ne number of Section		[1]
(i	iii)	The table shows the		tickets sold in each section.	[1]
(i	iii)	The table shows the	Section	tickets sold in each section.  Number of tickets sold	[1]
(i	iii)	The table shows the	Section A	Number of tickets sold	[1]
(i	iii)		Section  A  B  C	Number of tickets sold  120  136  30	[1]
(i	iii)		Section  A  B  C	Number of tickets sold  120  136	[1]
(i	iii)		Section  A  B  C	Number of tickets sold  120  136  30	[1]
(i	iii)		Section  A  B  C	Number of tickets sold  120  136  30	[1]
(i	iii)		Section  A  B  C	Number of tickets sold  120  136  30	[1]

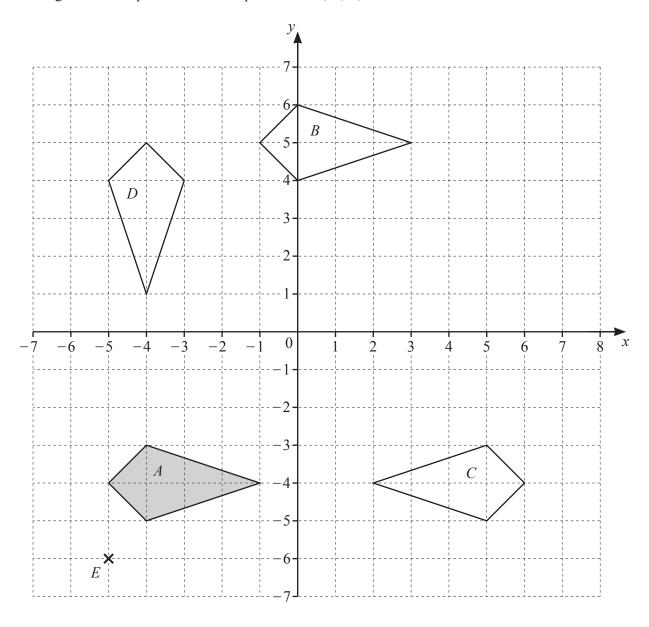
(iv) The concert costs \$4500 to organise.

Calculate the amount received from the ticket sales as a percentage of the \$4500.

..... % [1]

\$.....[3]

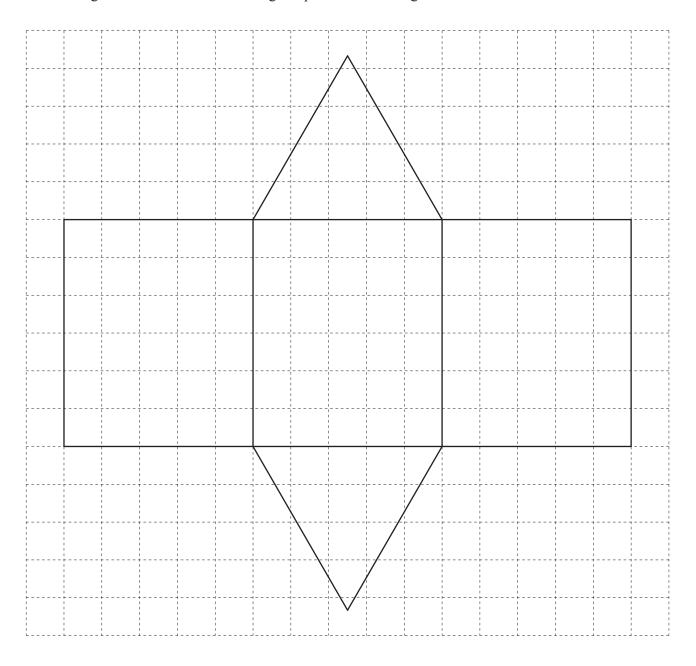
2 The grid shows a point E and four quadrilaterals, A, B, C and D.



(a) Write down the mathematical name of shape A.

(b)	Des	cribe fully the <b>single</b> transformation that maps	
	(i)	shape $A$ onto shape $B$ ,	
			[2]
	(ii)	shape $A$ onto shape $C$ ,	
			[2]
(	(iii)	shape $A$ onto shape $D$ .	
			[3]
(c)	(i)	Write down the coordinates of the point $E$ .	
		()	[1]
	(ii)	On the grid, draw the image of shape $A$ after an enlargement by scale factor 3, centre $E$ .	[2]

The diagram shows the net of a triangular prism on a 1 cm<sup>2</sup> grid. 3



(a) \(\frac{1}{2}\)	Write down	the mathematical	name for th	e type of tria	ingle shown or	n the grid.
---------------------	------------	------------------	-------------	----------------	----------------	-------------

.....[1]

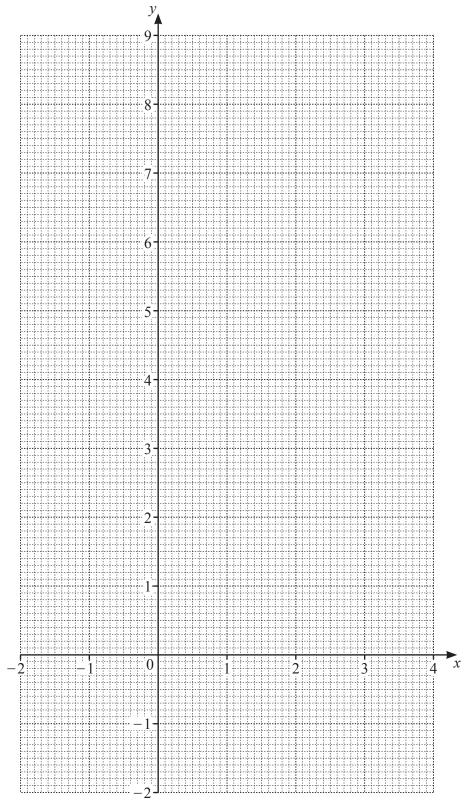
b) (i)	Measure the perpendicular height of the triangle.	
(ii)	Calculate the area of the triangle.	cm [1]
(iii)	Calculate the volume of the triangular prism.	cm <sup>2</sup> [2]
		cm <sup>3</sup> [2]

4 (a) Complete the table of values for  $y = 7 + 2x - x^2$ .

x	-2	-1	0	1	2	3	4
у	-1			8	7		-1

[2]

**(b)** On the grid, draw the graph of  $y = 7 + 2x - x^2$  for  $-2 \le x \le 4$ .



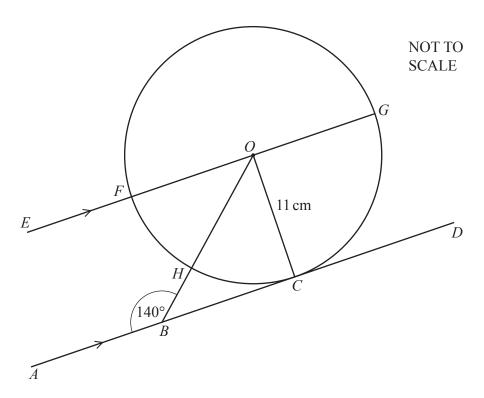
(c)	Write down the equation of the line of	f symmetry of the g	graph.	
(d)	Use your graph to solve the equation	$7 + 2x - x^2 = 0.$		[1]
			x =  or $x =$	[2]

	ng the integers from 60 to 75 only, find	
(i) (ii)	a multiple of 17, the prime numbers.	 [1]
<b>(b)</b> Fin		 [2]
(i) (ii)	the square root of 4489, $4^{3},$	 [1]
(iii)	$\sqrt[3]{274625}$ ,	 [1]
(iv)	$2^{-3} \times 24^2$ .	 [1]
		 [1]

5

(c)	Wri	te down the reciprocal of 7.	
( D)	***	[1	]
(d)	Wrı	te 3.72194 correct to 3 decimal places.	
		[1	]
(e)	Fine	d the lowest common multiple (LCM) of 8 and 14.	
		[2	.]
<b>(f)</b>	The	average temperature at the North Pole is $-23$ °C in January and $-11$ °C in March.	
	(i)	Find the difference between these temperatures.	
		°C [1	1
			J
	(ii)	The average temperature in July is 28 °C higher than the average temperature in March.	
		Find the average temperature in July.	
		°C [1	]

6



The diagram shows a circle, centre O, radius 11 cm. C, F, G and H are points on the circumference of the circle. The line AD touches the circle at C and is parallel to the line EG. B is a point on AD and angle  $ABO = 140^{\circ}$ .

(a) Write down the mathematical name of the straight line	AD.
---	-----

.....[1]

(b) (i) Find, in terms of  $\pi$ , the circumference of the circle.

..... cm [2]

(ii) Work out angle *FOH*.

Angle  $FOH = \dots$  [2]

(iii) Calculate the length of the minor arc FH.

..... cm [2]

c)	(i)	Give a reason why angle <i>BCO</i> is 90°.	
			[1]
	(ii)	Show that $BC = 13.11$ cm, correct to 2 decimal places.	
			[3]
	(iii)	Calculate <i>BH</i> .	

*BH* = ...... cm [3]

7 (a) 20 students from College A each run 5 km. The times, correct to the nearest minute, are recorded.

32	51	25	40	47	21	37	32	48	36
46	39	30	29	44	39	53	35	40	31

(i) Complete the stem-and-leaf diagram.

2	
3	
4	
5	

Key: 3 | 4 represents 34 minutes

[2]

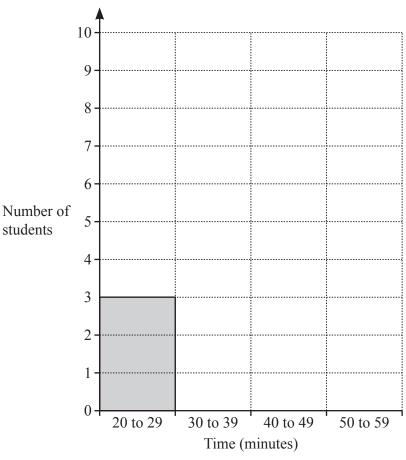
(ii) Find the range of the times.

 min	[1]

(iii) Find the median of the times.



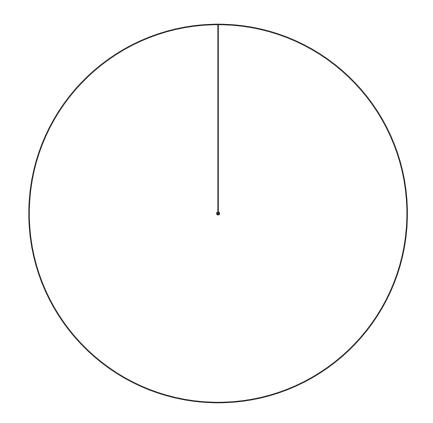
(iv) Complete the bar chart for the times of the students.



**(b)** 20 students from College B each run 5 km. Their times, correct to the nearest minute, are recorded and the results are shown in the table.

Time (minutes)	Number of students	Pie chart sector angle
30 to 39	5	90°
40 to 49	8	
50 to 59	7	

(i) Complete the table. [2]



[2]

(c) Write down two comments comparing the times of students from College A with the times of students from College B.

1	
2	
_	
	[2]

8	(a)	Simplify	3c - 5d - c + 2d.
U	(**)	Simping	30 30 0 1 20.

	. [2]

**(b)** Solve the equation 12x - 7 = 23.

$$x = \dots$$
 [2]

(c) Multiply out. 9(3-x)

 $(\mathbf{d}) \qquad A = \frac{(a+b)h}{2}$ 

Work out the value of h when A = 38.64, a = 5.5 and b = 3.7.

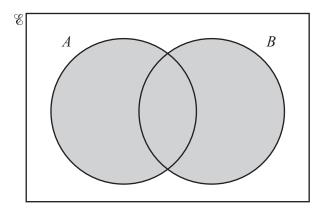
$$h = \dots [3]$$

)	Three times Alphonse's age is equal to 5 times Beatrice's age.  Twice Beatrice's age is 4 years more than Alphonse's age.					
	(i)	Use this information to write down two equations in $x$ and	d y.			
				[2]		
	(ii)	Find the age of Alphonse and the age of Beatrice.				

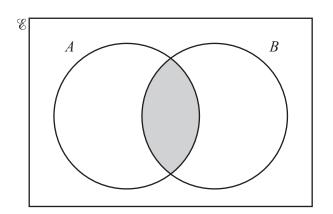
Alphonse ..... years old

Beatrice ..... years old [3]

9 (a) Use set notation to describe the shaded region in each Venn diagram.



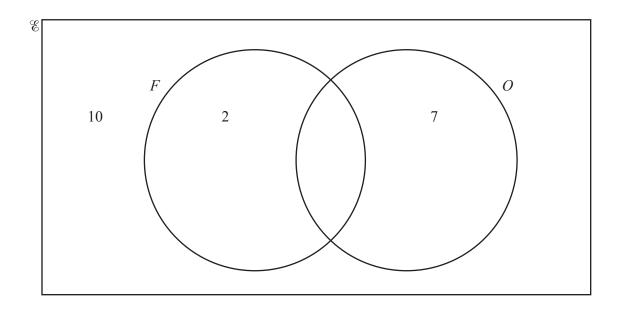
.....



.....

[2]

- (b)  $\mathscr{E} = \{x : x \text{ is a natural number } \le 15\}$   $F = \{x : x \text{ is a factor of } 12\}$   $O = \{x : x \text{ is an odd number}\}$ 
  - (i) Complete the Venn diagram to show the elements of these sets.



[2]

(11)	Write down one number that is in set $O$ , but not in set $F$ .	
(iii)	Find $n(F \cup O)$ .	 [1]
(iv)	A number is chosen at random from $\mathscr{E}$ .  Work out the probability that this number is in set $O$ .	 [1]
		[1]
		 [1]

Question 10 is printed on the next page.

- 10 Point B is 36 km from point A on a bearing of  $140^{\circ}$ .
  - (a) Using a scale of 1 centimetre to represent 4 kilometres, mark the position of B.



Scale: 1 cm to 4 km

[2]

(b) (i) Point C is 28 km from A and 20 km from B. The bearing of C from A is less than 140°.

**Using a ruler and compasses only**, construct triangle *ABC*. Show all your construction arcs.

[3]

(ii) Measure angle ACB.

Angle  $ACB = \dots$  [1]

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which itself is a department of the University of Cambridge.

© UCLES 2020