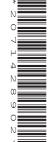


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MATHEMATICS 0580/43

Paper 4 (Extended) May/June 2020

2 hours 30 minutes

You must answer on the question paper.

You will need: Geometrical instruments

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For π , use either your calculator value or 3.142.

INFORMATION

- The total mark for this paper is 130.
- The number of marks for each question or part question is shown in brackets [].

This document has 24 pages. Blank pages are indicated.

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[Turn over

| (b) In September the total income at the campsite was \$37054. This was a decrease of 4.5% on the total income in August. Calculate the total income in August. (c) The visitors to the campsite today are in the ratio men: women = 5:4 and women: children = 3:7. | | 2 | |
|--|-----|---|--------------|
| Today there are 54 tents and 18 caravans on the site. Calculate the fees charged today. \$ | (a) | (per day) Tent \$15.00 | |
| Calculate the fees charged today. \$ | | | |
| (b) In September the total income at the campsite was \$37054. This was a decrease of 4.5% on the total income in August. Calculate the total income in August. (c) The visitors to the campsite today are in the ratio men: women = 5:4 and women: children = 3:7. | | Calculate the fees charged today. | |
| (c) The visitors to the campsite today are in the ratio men: women = 5:4 and women: children = 3:7. | (b) | This was a decrease of 4.5% on the total income in August | |
| men: women = $5:4$ and women: children = $3:7$. | | | \$[2] |
| | (c) | The visitors to the campsite today are in the ratio | |
| (i) Calculate the ratio men: women: children in its simplest form. | | men: women = $5:4$ and women: chil | dren = 3:7. |
| 1 | | (i) Calculate the ratio men: women: children in its sin | mplest form. |
| | | | : : |

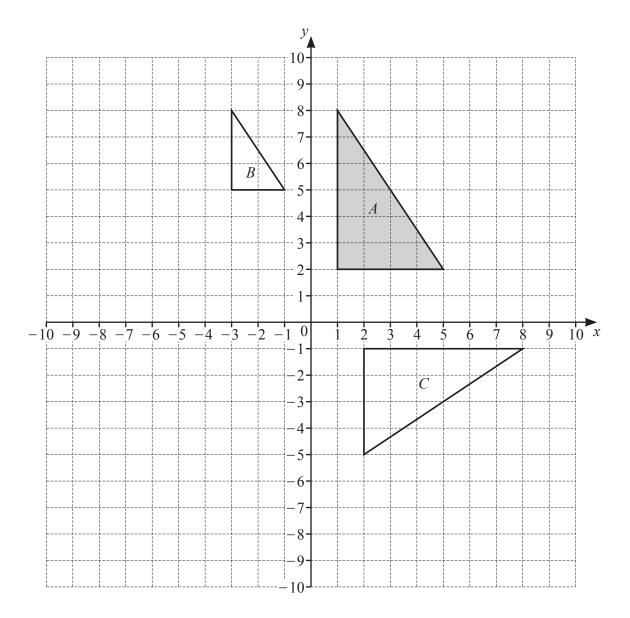
Today there are 224 children at the campsite.

Calculate the total number of men and women.

.....[3]

| (d) | The space allowed for each tent is a rectangle measuring 8 m by 6 m, each correct to the nearest metre. |
|-----|---|
| | Calculate the upper bound for the area of the space allowed for each tent. |
| | |
| | |
| | m^2 [2] |
| (e) | The value of the campsite has increased exponentially by 1.5% every year since it opened 30 years ago. |
| | Calculate the value of the campsite now as a percentage of its value 30 years ago. |
| | |
| | |
| | |
| | |
| | % [2] |
| | |

2



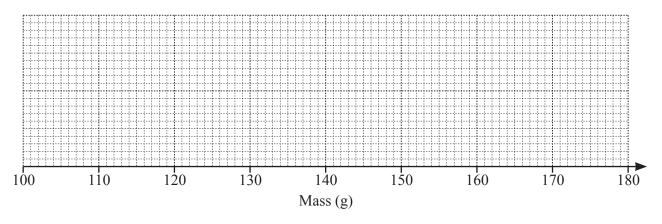
- (a) (i) Draw the image of triangle A after a reflection in the line y = -x. [2]
 - (ii) Draw the image of triangle A after a translation by the vector $\begin{pmatrix} -2 \\ -9 \end{pmatrix}$. [2]
- **(b)** Describe fully the **single** transformation that maps
 - (i) triangle A onto triangle B,

(ii) triangle A onto triangle C.

.....

- 3 (a) Here is some information about the masses of potatoes in a sack:
 - The largest potato has a mass of 174 g.
 - The range is 69 g.
 - The median is 148 g.
 - The lower quartile is 121 g.
 - The interquartile range is 38 g.

On the grid below, draw a box-and-whisker plot to show this information.



[4]

(b) The table shows the marks scored by some students in a test.

| Mark | 5 | 6 | 7 | 8 | 9 | 10 |
|-----------|---|---|----|---|---|----|
| Frequency | 8 | 2 | 12 | 2 | 0 | 1 |

Calculate the mean mark.

.....[3]

| 4 | (a) | Solve the inequality. | |
|---|-----|-----------------------|-------------------|
| | | | $3m+12 \leq 8m-5$ |

| LJ. |
|--------|
| 14 |

(b) Solve the equation.
$$\frac{2x+5}{3-x} = \frac{14}{15}$$

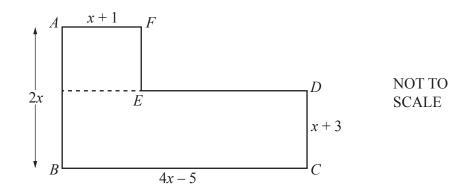
$$x =$$
 [3]

(c) Solve the simultaneous equations. You must show all your working.

$$y = 4 - x$$
$$x^2 + 2y^2 = 67$$

| $x = \dots,$ | <i>y</i> = | |
|--------------|------------|---------|
| $x = \dots,$ | y = | [6] |

5 All the lengths in this question are in centimetres.



The diagram shows a shape ABCDEF made from two rectangles. The total area of the shape is 342 cm^2 .

(a) Show that $x^2 + x - 72 = 0$.

[5]

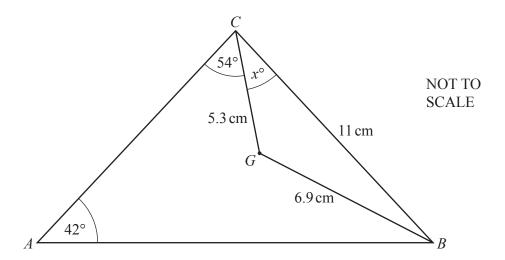
(b) Solve by factorisation.

$$x^2 + x - 72 = 0$$

$$x = \dots$$
 or $x = \dots$ [3]

| (c) | Work out the perimeter of the shape <i>ABCDEF</i> . |
|-----|---|
| | |
| | |
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| | |
| | |
| | am [2] |
| | cm [2] |
| (d) | Calculate angle <i>DBC</i> . |
| | |
| | |
| | |
| | |
| | |

6 (a)



The diagram shows triangle ABC with point G inside. CB = 11 cm, CG = 5.3 cm and BG = 6.9 cm. Angle $CAB = 42^{\circ}$ and angle $ACG = 54^{\circ}$.

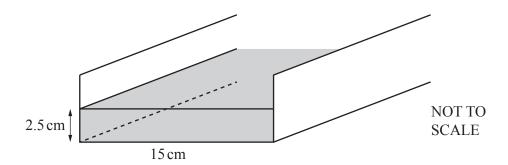
| (i) Calculate the value of | | | | _ | | | - | |
|----------------------------|-----|-------|---------|-------|-------|------|-----|---|
| THE CALCIDATE THE VALUE OF | (:) | (((| laulata | th a | T 7.0 | 1110 | af. | - |
| | | ı (a | исппате | 11110 | Val | ше | () | X |

| x = | [4] |
|-----|---------|

(ii) Calculate AC.

$$AC = \dots$$
 cm [4]

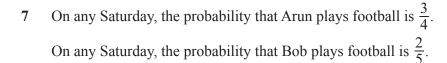
(b)



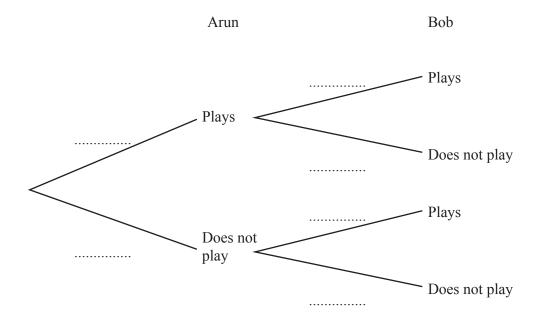
Water flows at a speed of $20 \, \text{cm/s}$ along a rectangular channel into a lake. The width of the channel is $15 \, \text{cm}$. The depth of the water is $2.5 \, \text{cm}$.

Calculate the amount of water that flows from the channel into the lake in 1 hour. Give your answer in litres.

| litres | [4] |
|------------|-----|



(a) (i) Complete the tree diagram.



(ii) Calculate the probability that, one Saturday, Arun and Bob both play football.

.....[2]

[2]

(iii) Calculate the probability that, one Saturday, either Arun plays football or Bob plays football, but not both.

.....[3]

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| (b) | Calculate the probability that Bob plays football for 2 of the next 3 Saturdays. | |
|-----|--|-----|
| | | |
| | | |
| | | |
| | | [3] |
| (c) | When Arun plays football, the probability that he scores the winning goal is $\frac{1}{7}$. | |
| | Calculate the probability that Arun scores the winning goal one Saturday. | |
| | | |
| | | |
| | | |
| | | |
| | | [2] |
| | | |

| 8 (a) The interior angle of a regular polygon with n sides | is 150° |
|--|---------|
|--|---------|

Calculate the value of n.

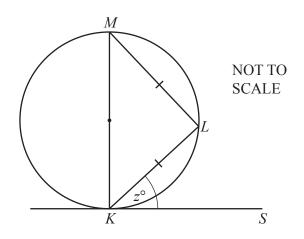
| n — | ГЭ | 1 |
|-----|---------|---|
| n = | 4 | , |

(b) (i) K, L and M are points on the circle.

KS is a tangent to the circle at K.

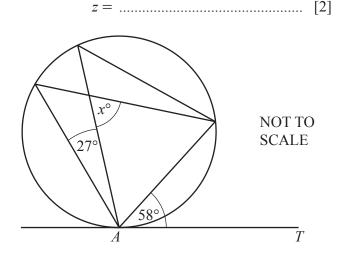
KM is a diameter and triangle KLM is isosceles.

Find the value of z.



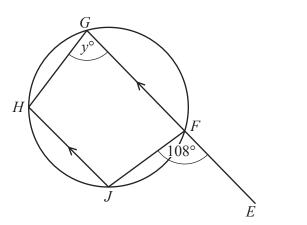
(ii) AT is a tangent to the circle at A.

Find the value of x.



$$x = \dots$$
 [2]

(iii)



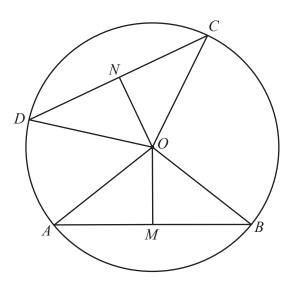
NOT TO SCALE

F, G, H and J are points on the circle. EFG is a straight line parallel to JH.

Find the value of *y*.

 $y = \dots$ [2]

(c)



NOT TO SCALE

A, B, C and D are points on the circle, centre O. M is the midpoint of AB and N is the midpoint of CD. OM = ON

| Explain, | giving reasons | , why triangle | <i>OAB</i> is congruent to | triangle <i>OCD</i> . |
|----------|----------------|----------------|----------------------------|-----------------------|
| | | | | |

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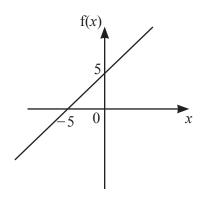
| 9 | (a) | The | equation of line <i>L</i> is $3x - 8y + 20 = 0$. |
|---|-----|------|--|
| | | (i) | Find the gradient of line L . |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | [2] |
| | | (ii) | Find the coordinates of the point where line L cuts the y -axis. |
| | | (11) | That the coordinates of the point where the L cuts the y-axis. |
| | | | |
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| (b) | The | coordinates of P are $(-3, 8)$ and the coordinates of Q are | e (9, -2). | |
|------------|-------|---|-------------------------------|-----|
| | (i) | Calculate the length <i>PQ</i> . | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | [3] |
| | (ii) | Find the equation of the line parallel to PQ that passes t | through the point $(6, -1)$. | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | [3] |
| (| (iii) | Find the equation of the perpendicular bisector of <i>PQ</i> . | | |
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| | | | | |
| | | | | [4] |
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| | | | | |

10 (a) The diagrams show the graphs of two functions.

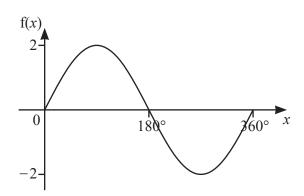
Write down each function.

(i)



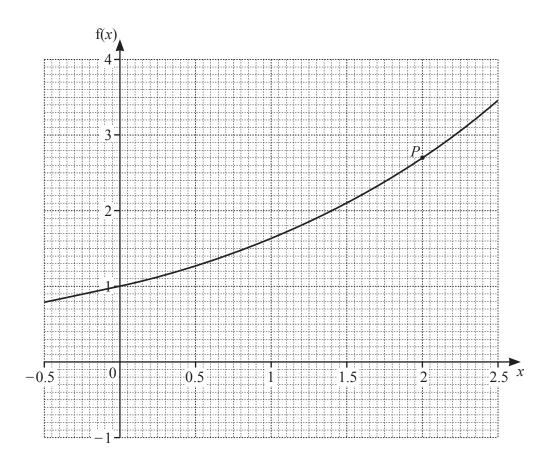
$$f(x) =$$
 [2]

(ii)



$$f(x) = \dots [2]$$

(b)



The diagram shows the graph of another function.

By drawing a suitable tangent, find an estimate for the gradient of the function at the point *P*.

.....[3]

$$f(x) = 7x - 4$$

$$g(x) = \frac{2x}{x-3}, x \neq 3$$

$$h(x) = x^2$$

(a) Find g(6).

| | [1] |
|---|-----------|
| • | F - 1 |

(b) Find fg(4).



(c) Find fh(x).



(d) Find $\frac{f(x)}{2} + g(x)$.

Give your answer as a single fraction, in terms of x, in its simplest form.

......[3]

| (e) | Find the value of x when $f(x+2) = -$ | 11. | | |
|------------|--|--------------|------------|-----|
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| | | | | |
| | | | <i>x</i> = | [2] |
| (f) | Find the values of p that satisfy $h(p) =$ | = <i>p</i> . | | |
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| | | | | |
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| | | | | |
| | | | | [2] |
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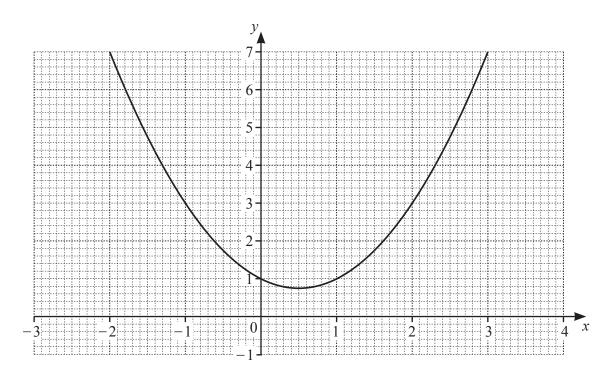
| 12 | (a) | A curve has equation | $v = 4x^3 - 3x + 3$ |
|----|-----|----------------------|---------------------|
| 14 | (a) | A curve has equation | y = 4x - 3x + |

(i) Find the coordinates of the two stationary points.

(ii) Determine whether each of the stationary points is a maximum or a minimum. Give reasons for your answers.

[3]

(b) The graph of $y = x^2 - x + 1$ is shown on the grid.



By drawing a suitable line on the grid, solve the equation $x^2 - 2x - 2 = 0$.

 $x = \dots$ or $x = \dots$ [3]

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